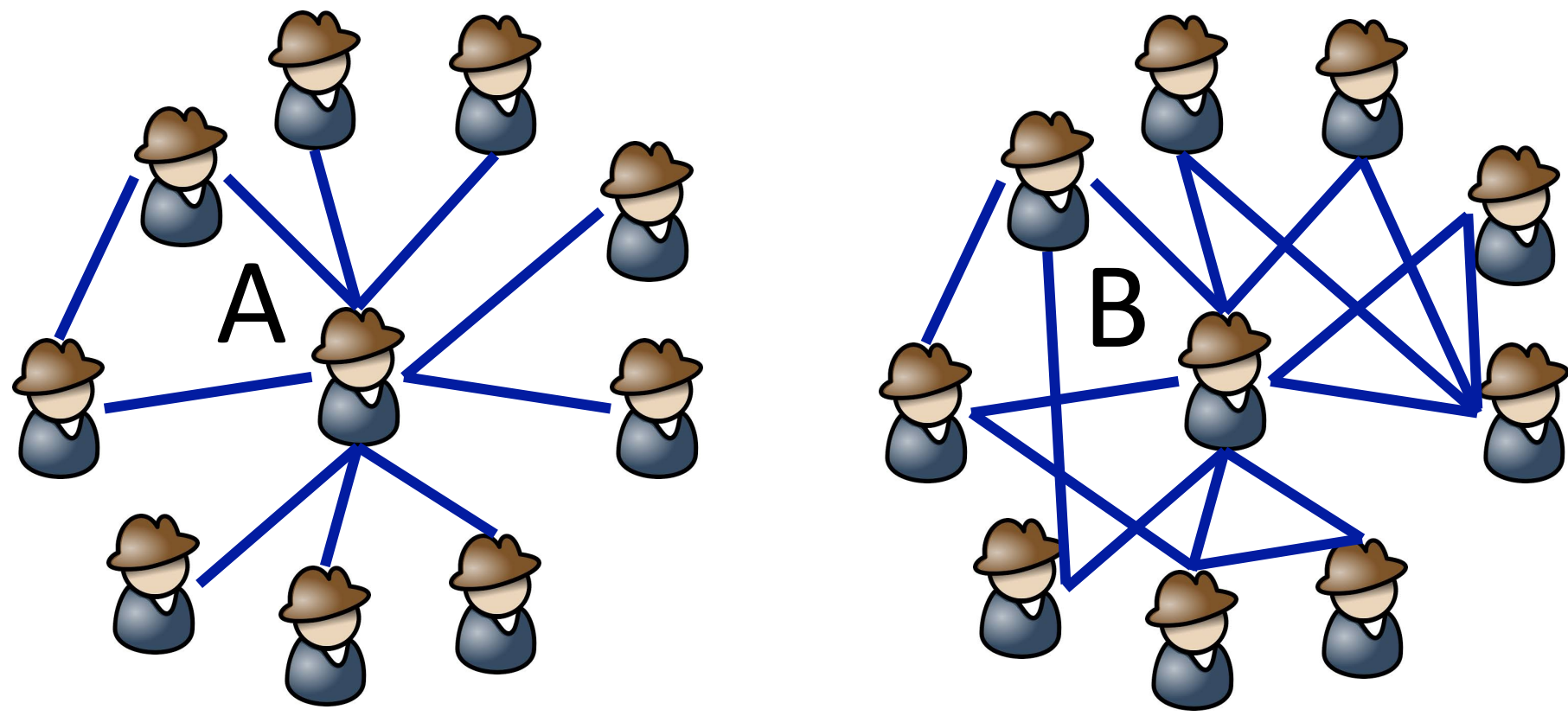


Role-aware Conformity Influence Modeling and Analysis in Social Networks

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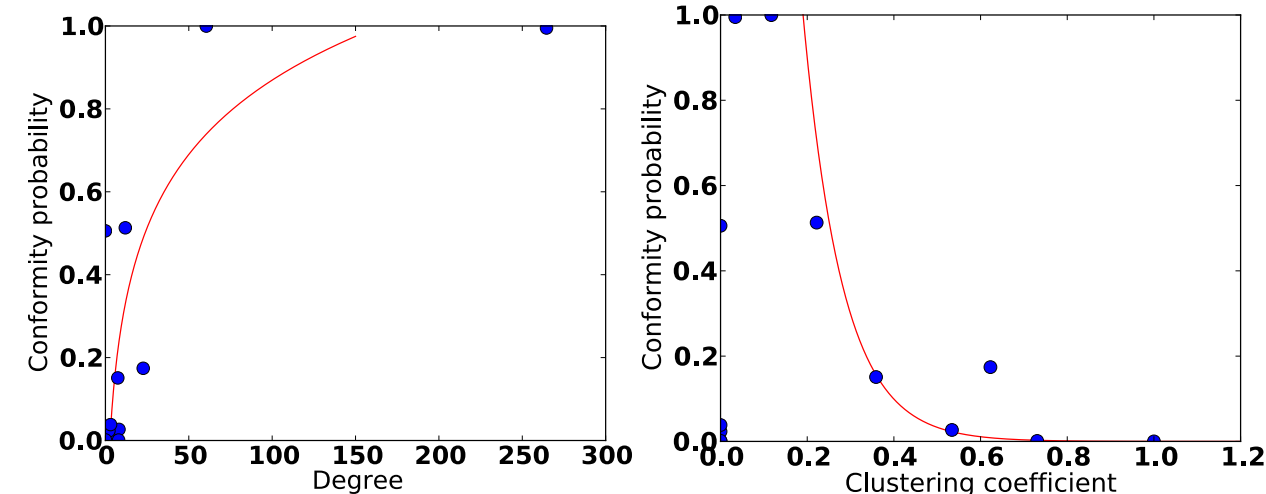
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1. Problem



Question: Who is more likely to conform to others, A or B?

Result



The persons with higher degree and lower clustering coefficient are more likely to conform to others.

2. Prediction

- Data Set: We select eight domains from computer science, and collect papers (title, authors, citation relationships) from the well-known journals/conferences in the domain. 231,728 papers, 269,508 authors, and 347,735 citations.
- Prediction Task: predict whether a user will write a given word in her paper title in a given time period.

- Baseline Methods:

- PLSA : ignore conformity tendency.
- CIM : conformity tendency is learned for each person.
- RCM(our method): conformity tendency is learned for each role.

Method	P@5	MAP	AUC
PLSA	17.49	8.49	78.85
CTM	21.75	11.31	85.13
RCM	24.36	12.07	85.95

3. Formalize Conformity Influence

Conformity Theory [Bernheim 1994]

- Everyone in a group express her own individuality.
- Yet, even individualists pursue somewhat for status (esteem or popularity) and change their choices toward the social norm.

Utility Function

Intrinsic utility + conformity utility

$$f(y_i) = (1 - \lambda_i) d(y_i, \hat{y}_i) + \lambda_i \sum_{j \in N(i)} d(y_i, y_j)$$

- y_i : a binary value to represent whether a user v_i adopts an action or not.
- \hat{y}_i : the intrinsic preferred selection of user v_i .
- $N(i)$: neighbors of v_i at the time when v_i makes the decision.
- $d(\cdot, \cdot)$: a metric that gives a utility of 1 when two decisions are the same, and 0 otherwise.
- λ_i : the conformity tendency of user v_i .

Nash Equilibria

There exists Nash equilibria if all users in a network make the decisions for a given action according to the utility function.

Proof:

1. When there is only one user in a network, the proof is straightforward.
2. When there are two users in a network,
 - If their intrinsic preferences are the same, a Nash equilibrium exists because they will make the same decision.
 - If their intrinsic preferences are different, λ determines the final selection.
 - $\lambda < 0.5$, a Nash equilibrium exists because they will select their own preferences respectively.
 - $\lambda > 0.5$, two Nash equilibria exist because they will both select the intrinsic preference \hat{y}_1 or \hat{y}_2 .
3. We use induction method to prove if a Nash equilibrium exists in a k -network, a Nash equilibrium will definitely exist in any $(k+1)$ -network.
 - The general idea is to investigate whether the neighbors of v_{k+1} will change their decisions when v_{k+1} joined a k -network that has already arrived at a Nash equilibrium.

4. Measure Conformity Influence

Utility Function Extension

- To solve data sparsity problem in real applications, we extend the utility function by incorporating role and topic.
 - **Role r** : Conformity tendency is different for persons with different roles.
 - **Topic z** : Conformity tendency is different on actions with different topics.
 - Binary action y_i is extended to a set of actions $\{w\}$.
- When in role r , the utility function of v_i taking an action w is :

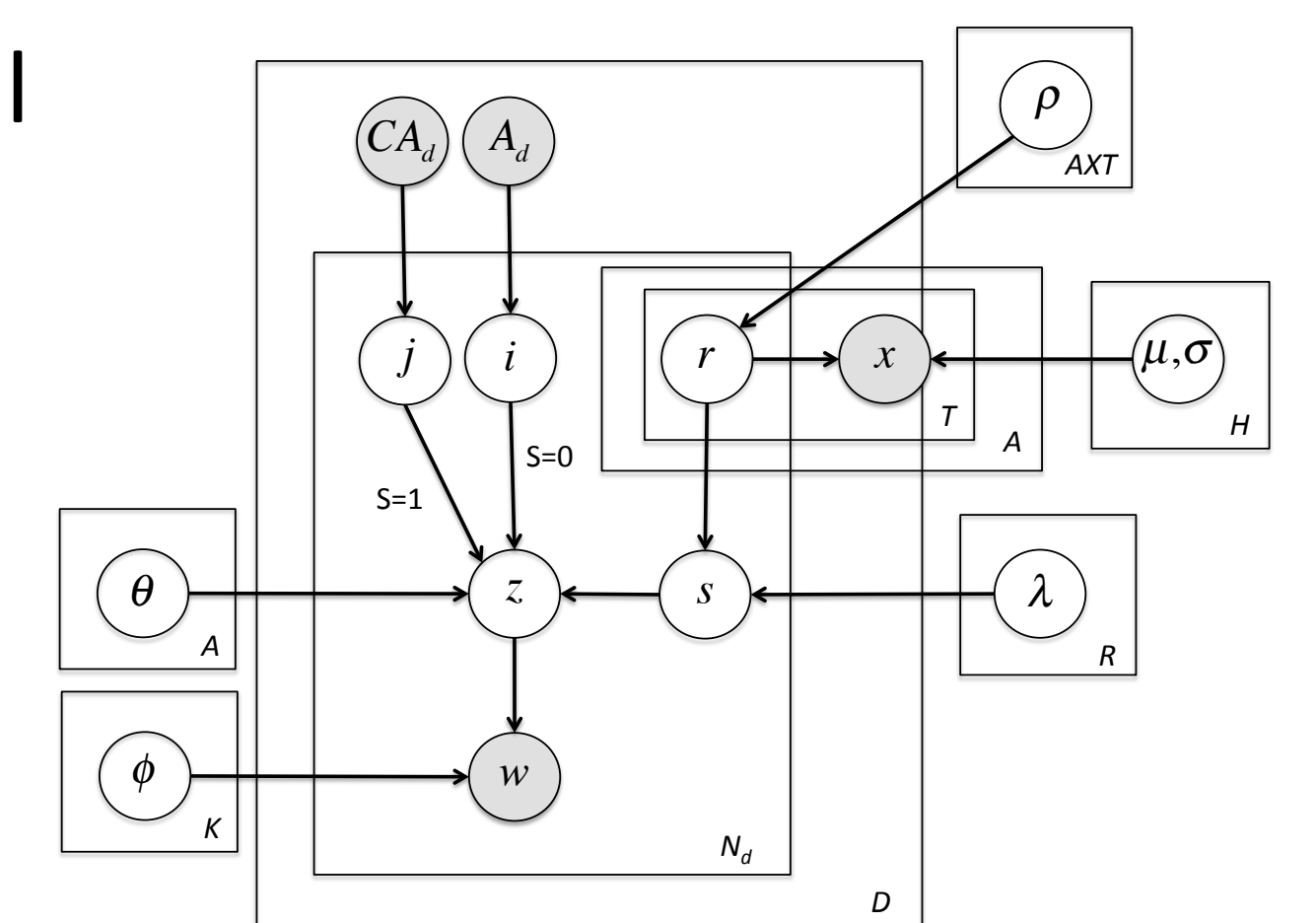
$$\gamma_{i,r}^w = \left[(1 - \lambda_r) \sum_{z=1}^K \theta_i^z \phi_z^w + \lambda_r \frac{1}{|N_i|} \sum_{j \in N_i} \sum_{z=1}^K \theta_j^z \phi_z^w \right]$$

- θ_i^z : the probability of user v_i choosing topic z .
- ϕ_z^w : the probability of taking action w under topic z .
- λ_r : the conformity tendency of role r .

Model Intuition

- The first part models the generation of individual attributes \mathbf{x} .

- For an attribute, we first draw a role from a multinomial distribution, and then draw x from a normal distribution with respect to r .



- The second part models the total utility of generating all the actions \mathbf{w} .

- For an action, we first toss a coin s with distribution $\text{Bern}(\lambda_r)$. Then, if $s = 1$, w is determined by individual's intrinsic topic distribution. Otherwise, w is influenced by the neighbors' topic distributions.

Model Learning

- To estimate λ_r , i.e., the conformity over role.
- By maximizing the likelihood of generating both the **individual attributes** and the **actions**.

$$\mathcal{L}_1 = \prod_{i=1}^A \prod_{t=1}^T \prod_{h=1}^H \sum_{r=1}^R \frac{\rho_{i,t}^r}{\sqrt{2\pi\sigma_{r,h}^2}} \exp \left[-\frac{(x_{i,t,h} - \mu_{r,h})^2}{2\sigma_{r,h}^2} \right] \quad \mathcal{L}_2 = \prod_{d,w} \sum_{i \in A_d} \frac{\sum_{r=1}^R \rho_{i,t}^r \gamma_{r,i}^w}{|A_d|}$$