# Learning to Infer Social Ties in Large Networks

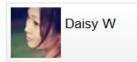
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## Real social networks are complex...

- Nobody exists only in one social network.
  - Public network vs. private network
  - Business network vs. family network
- However, existing networks (e.g., Facebook and Twitter) are trying to lump everyone into one big network
  - FB tries to solve this problem via lists/groups
  - However...
- Google+







which circle? Users do not take time to create it.





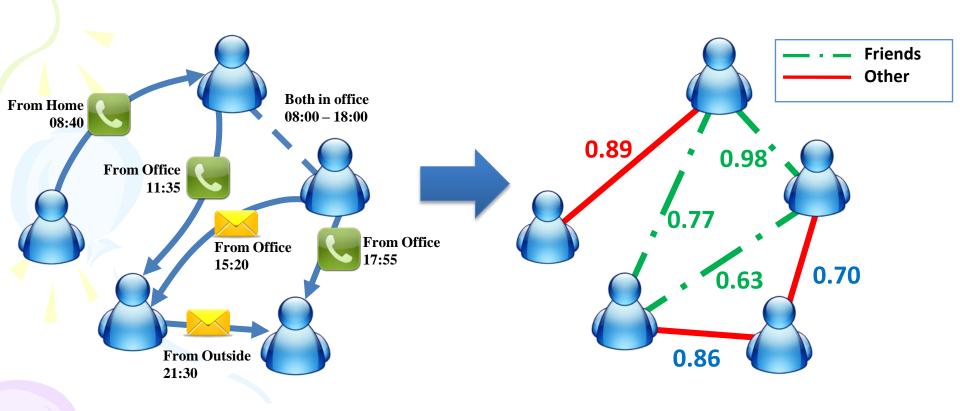


## Even complex than we imaged!

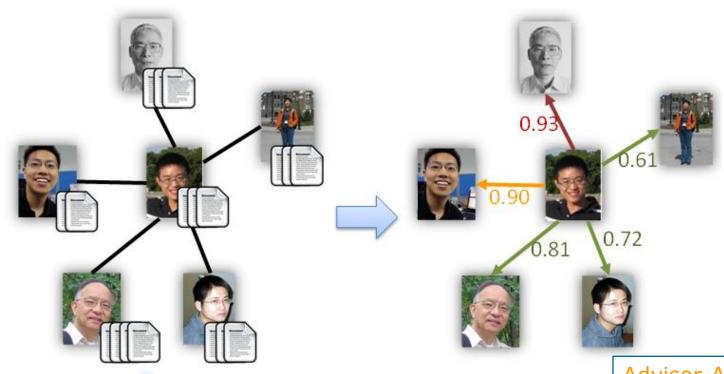
- Only 16% of mobile phone users in Europe have created custom contact groups
  - users do not take the time to create it
  - users do not know how to circle their friends

 The fact is that our social network is black-white...

## Example: Mobile network



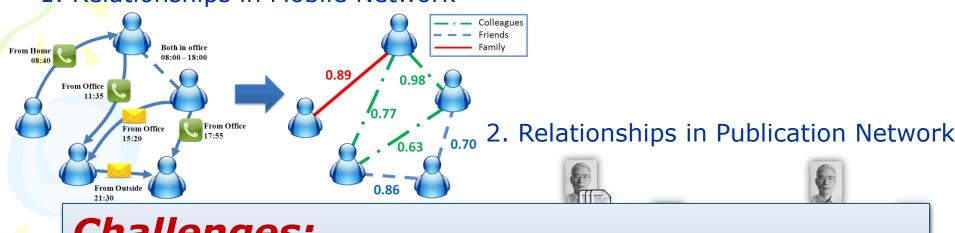
## Example: Coauthor networks



Advisor-Advisee Advisee-Advisor Coauthor

## Challenges

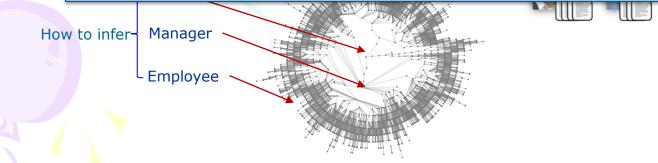
1. Relationships in Mobile Network



#### Challenges:

3.

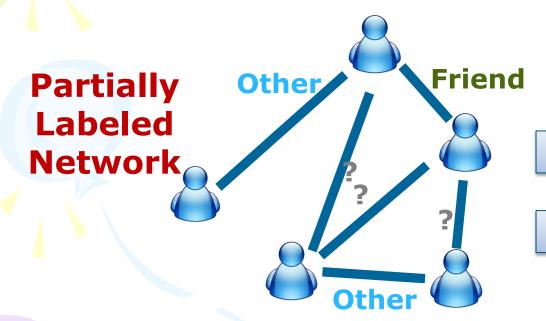
- A generalized framework for inferring social ties?
- A scalable, efficient method?



Advisor-Advisee Advisee-Advisor Coauthor

#### Problem Formulation

Input:  $G = (V E^{L})(R^{L})(R^{L})(W)$ 



V: Set of Users

 $E^L$ ,  $R^L$ : Labeled relationships

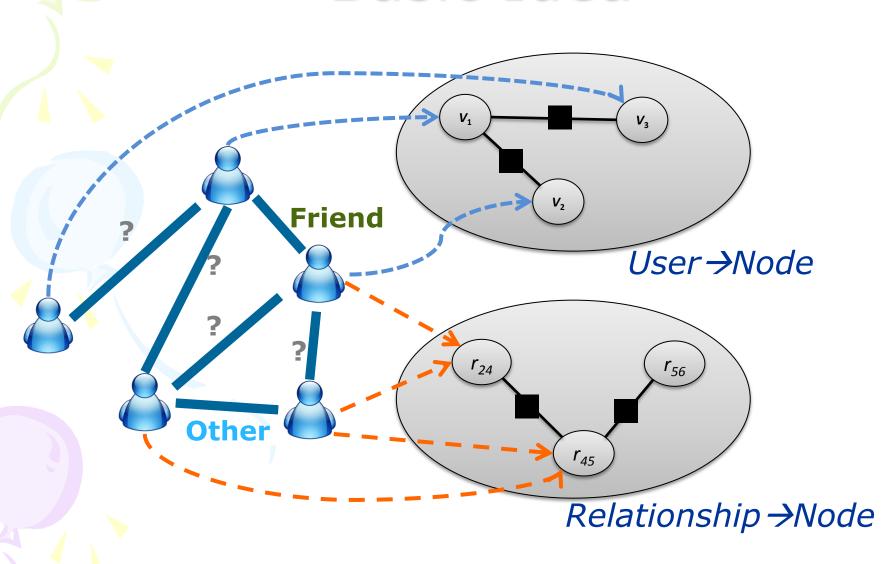
E<sup>U</sup>: Unlabeled relationships

Input:  $G=(V,E^L,E^U,R^L,W)$ 

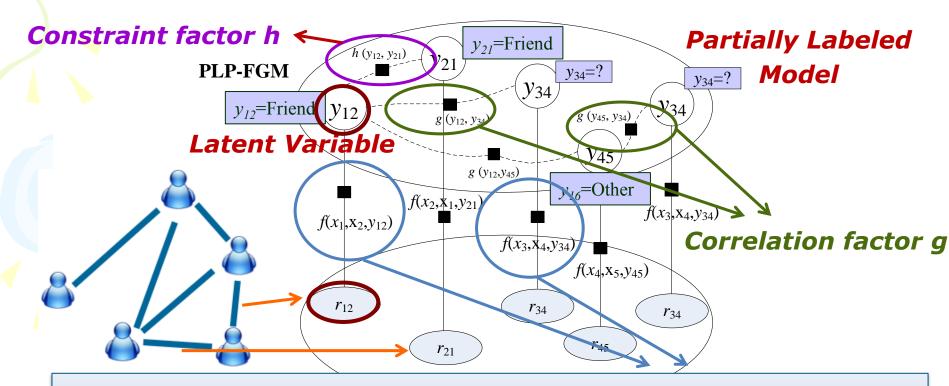


Output:  $f: G \rightarrow R$ 

### Basic Idea



## Partially Labeled Pairwise Factor Graph Model (PLP-FGM)



#### **Problem:**

Ma

For each relationship, identify which type has the highest probability?

## Solutions<sub>(con't)</sub>

- Different ways to instantiate factors
  - We use exponential-linear functions
    - Attribute Factor:

$$f(y_i, \mathbf{x}_i) = \frac{1}{Z_{\lambda}} \exp\{\lambda^T \Phi(y_i, \mathbf{x}_i)\}\$$

Correlation / Constraint Factor:

$$g(y_i, G(y_i)) = \frac{1}{Z_{\alpha}} \exp\{\sum_{y_j \in G(y_i)} \alpha^T \mathbf{g}(y_i, y_j)\}$$

$$h(y_i, H(y_i)) = \frac{1}{Z_{\beta}} \exp\{\sum_{y_i \in H(y_i)} \beta^T \mathbf{h}(y_i, y_j)\}\$$

$$- \quad \theta = [\lambda, \alpha, \beta], s = [\Phi^T, g^T, h^T]^T$$

Log-Likelihood of labeled Data:

$$\mathcal{O}(\theta) = \log \sum_{Y|Y^L} \exp\{\theta^T \mathbf{S}\} - \log \sum_{Y} \exp\{\theta^T \mathbf{S}\}$$

## Learning Algorithm

Maximize the log-likelihood of labeled relationships

Input: learning rate  $\eta$ 

Output: learned parameters  $\theta$ 

Initialize  $\theta$ ;

repeat

Calculate  $\mathbb{E}_{p_{\theta}(Y|Y^L,G)}$ S using LBP;

Calculate  $\mathbb{E}_{p_{\theta}(Y|G)}\mathbf{S}$  using LBP;

Calculate the gradient of  $\theta$  according to Eq. 7:

$$\nabla_{\theta} = \mathbb{E}_{p_{\theta}(Y|Y^{L},G)} \mathbf{S} - \mathbb{E}_{p_{\theta}(Y|G)} \mathbf{S}$$

Update parameter  $\theta$  with the learning rate  $\eta$ : Expectation Computing

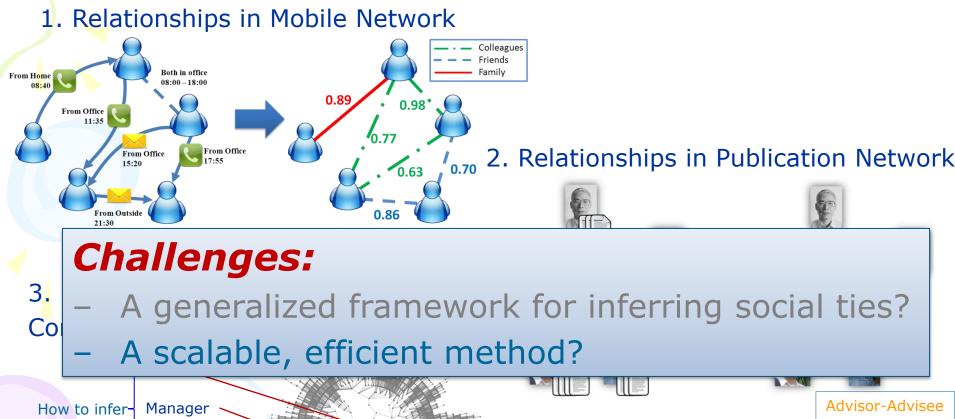
 $\theta_{\text{new}} = \theta_{\text{old}} - \eta \cdot \nabla_{\theta}$  Loopy Belief Propagation

until Convergence;

Algorithm 1: Learning PLP-FGM.

**Gradient Decent Method** 

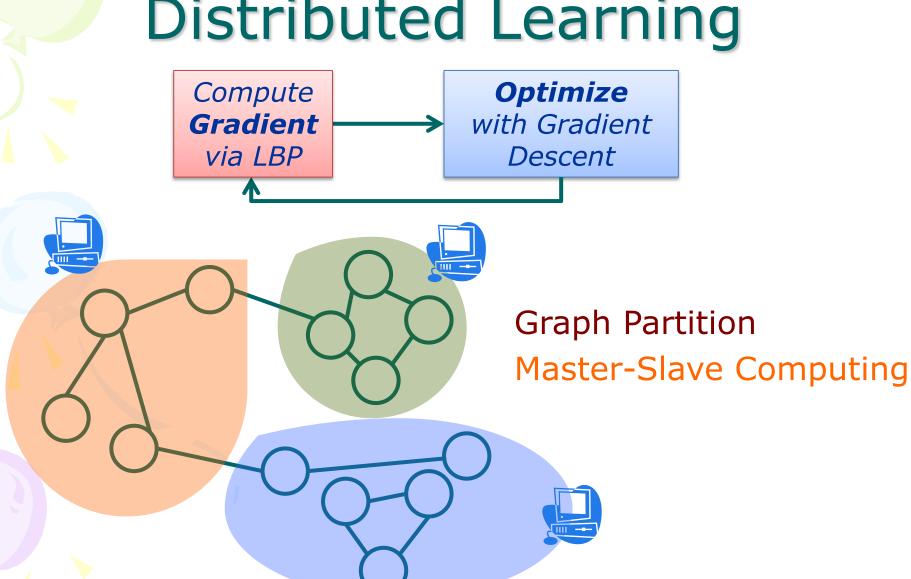
## Challenges



How to infer
Employee

Advisor-Advisee Advisee-Advisor Coauthor





#### **Data Sets**

- Coauthor Network (Publication)
  - To infer Advisor-Advisee relationship
  - Papers from DBLP
- Email Network (Email)
  - To infer Manger-Subordinate relationship
  - Using Enron Email Dataset
- Mobile Network (Mobile)
  - To infer Friendship
  - 107 users (ten-month). Published by MIT

Data Set	Users	Unlabeled Relationships	Labeled Relationships
Publication	1,036,990	1,984,164	6,096
Email	151	3,424	148
Mobile	107	5,122	314

#### Baselines

#### Baselines:

- SVM:
  - Use the same feature defined in our model to train a classification model

#### - TPFG:

- An unsupervised method to identify advisor-advisee relationships
- PLP-FGM-S
  - Do not use partially-labeled property
  - Train parameters on the labeled sub-graph

## Performance Analysis

Data Set	Method	Precision	Recall	F <sub>1</sub> -score
	SVM	72.5	54.9	62.1
Publication	TPFG	82.8	89.4	86.0
Publication	PLP-FGM-S	77.1	78.4	77.7
	PLP-FGM	91.4	87.7	89.5
	SVM	79.1	88.6	83.6
Email	PLP-FGM-S	85.8	85.6	85.7
	PLP-FGM	88.6	87.2	87.9
	SVM	92.7	64.9	76.4
Mobile	PLP-FGM-S	88.1	71.3	78.8
	PLP-FGM	89.4	75.2	81.6

**SVM**: Use the same feature to train a classification model

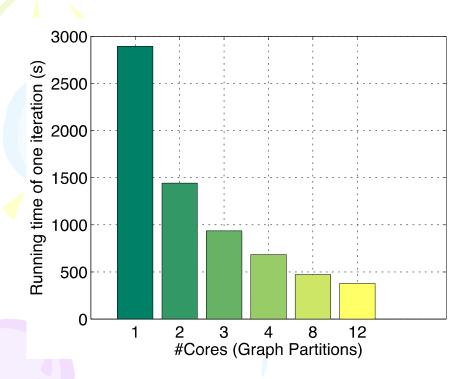
**TPFG**: An unsupervised method to identify advisor-advisee relationships

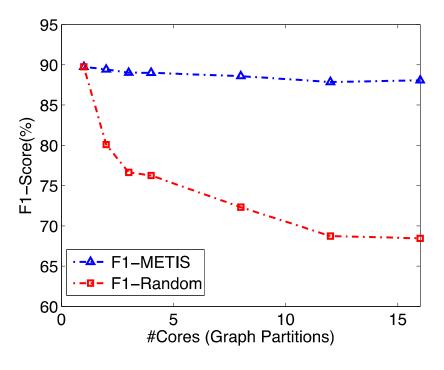
PLP-FGM-S: Train PLP-FGM model on the labeled sub-graph

## Factor Contribution Analysis

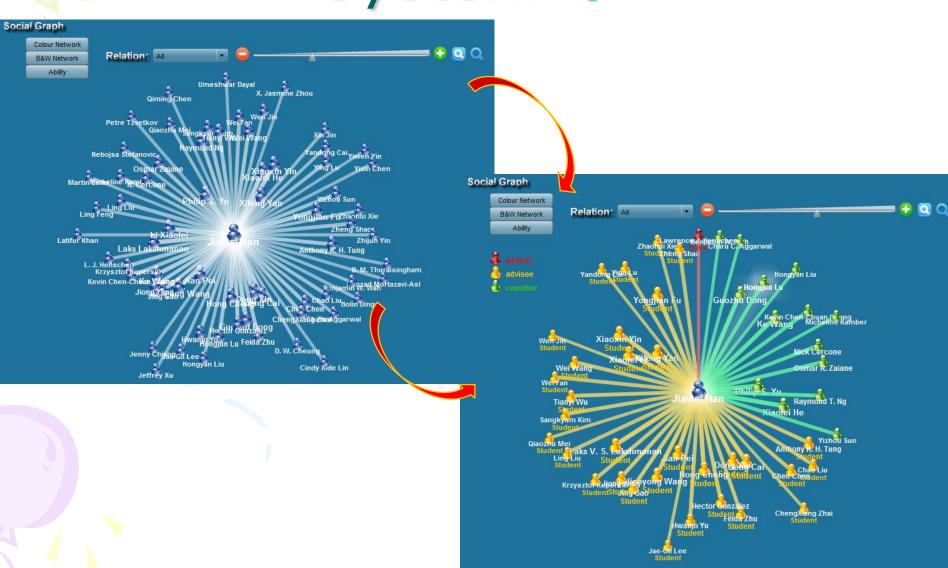
Data Set	Factor used	F <sub>1</sub> -score	
	Attributes	64.9	
Publication	+Co-advisor	75.0(+10.1%)	
Publication	+Co-advisee	74.7(+9.8%)	
	All	89.5(+24.6%)	
	Attributes	80.3	
	+Co-recipient	80.6(+0.3%)	
Email	+Co-manager	83.2(+2.9%)	
	+Co-subordinate	85.0(+4.7%)	
	All	87.9(+7.6%)	
	Attributes	80.2	
Mobile	+Co-location	80.4(+0.2%)	
Mobile	+Related-call	80.2(+0.0%)	
	All	81.6(+1.4%)	

### Distributed Learning Performance









#### Conclusion

- Formulate the problem of inferring the types of social ties
- Propose the PLP-FGM model to solve this problem, and present a distributed learning algorithm
- Validate the approach in different real data sets

### Future work

- Make online social networks colorful
  - How to involve user into learning process?
  - Connect with social theories?

## Thank you!

Any Questions?

#### Correlation Definition

- Mobile Dataset:
  - Co-location
    - 3 users in the same location.
  - Related-call
    - A Make a call to B&C at the same place/time
- For more information, please refer to the paper

## Feature Definition

Publication Paper count $ P_i ,  P_j $ Publication Coauthor ratio $ P_i / P_j $ Conference coverage The proportion of the conferences which both $v_i$ a tended among conferences $v_j$ attended.  First-paper-year-diff The difference in year of the earliest publication of the conference $v_j$ attended.	$v_j$ at-			
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First-paper-year-diff The difference in year of the earliest publication of				
	The difference in year of the earliest publication of $v_i$ and			
$  v_j $	$ v_j $ .			
Sender Recipients Include				
$v_i$ $v_j$				
Email Traffics $v_j$ $v_i$				
$v_i$ $v_k$ and not $v_j$				
$v_j$ $v_k$ and not $v_i$				
$v_k$ $v_i$ and not $v_j$				
$v_k$ $v_j$ and not $v_i$				
$v_k$ $v_i$ and $v_j$				
#voice calls The total number of voice call logs between two us	ers.			
" "	Number of messages between two users.			
	The proportion of calls at night (8pm to 8am).			
Mobile	The total duration time of calls between two users.			
#proximity The total number of proximity logs between two	The total number of proximity logs between two			
users.				
working hours (8am to 8pm).				

### Existing Methods...

- [Diehl:07] try to identify the relationships by learning a ranking function in Email network.
- Wang et al. [Wang:10] propose an unsupervised algorithm for mining the advisor-advisee relationships from the Publication network.
- Both algorithms focus on a specific domain
  - not easy to extend to other problems.